

Gaussian Noise Filtering From ECG Signal Using Improved Kalman Filter

¹Venkata Rami Reddy.D, ²Abdul Rahim.B, ³Fahimuddin.Shaik

^{1,2,3}Department of E.C.E, Annamacharya Institute of Technology & Sciences, Rajampet, A.P., India

Abstract: An electro cardio gram (ECG) signal is a series of waves and deflections which represents the electrical activity of the heart over time. ECG signal can be contaminated by different forms of noises. These noises mislead the ECG annotators from accurate identification of the ECG signal features. Conventional filters are used to reduce the noise components in ECG signal from different unwanted frequency components. But this filtering process is not efficiently work on the contaminated ECG signals. In biomedical signals reduction of noise is difficult with the fixed coefficients filters, because these signals are random in nature and not exact known depending on the time. To overcome this type of problem we require an adaptive algorithm technique. In this paper we present improved Kalman filter developed with a state space model and autocorrelation least squares(ALS) technique to estimate the state variables, including the Gaussian noise approximation from the previous values of the original ECG signal. This filter enhances the quality of the ECG signal and shows the good convergence properties. The results have been concluded with the MIT-BIH arrhythmia data base and MATLAB software.

Keywords: ECG signal, Gaussian noise, Adaptive algorithm, Kalman filter, SNR.

I. INTRODUCTION

Electrocardiogram (ECG) signal is an electrical manifestation of the contractility of the heart. Ambulatory ECG signal recordings obtained by placing electrodes on the body chest using invasive method. The ECG signal frequency ranges from 0.5 to 100 Hz [1]. ECG analysis is very important for the evolution of cardiac arrhythmia and it guides the condition of a normal heart beat. Fig1 represents an example of a normal ECG signal.

ECG is includes the valuable information about heart condition, but it is frequently corrupted by various noises such as power line interferences and harmonics from power mains, muscle contraction, respiration and electromyogram is mixed with ECG, baseline wander noise is occurred due to the variable connection between the skin and the connected electrodes [2]. Noise affects at both low-frequency and high frequency components. This noise component reduces the precision and accuracy of an ECG signal. Hence noise reduction from ECG signals is very important research and studied widely from many years.

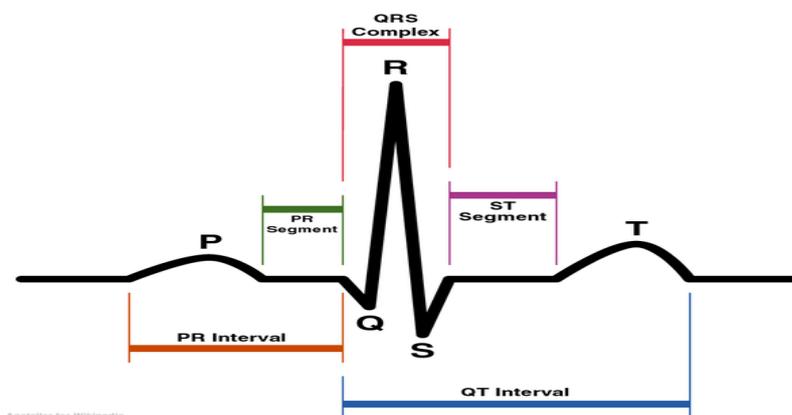


Fig 1: A typical ECG signal

II. LITERATURE SURVEY

ECG noise cancellation has long puzzled for the research community. Normal noise reduction methods are based on the standard filtering process techniques [1]-[4]. The ANC based on the Normalized LMS (NLMS) algorithm has a higher convergence rate than the algorithm used in normalized LMS algorithm [8]. The NLMS algorithm is also based on a fixed step size as used in the LMS algorithm. The authors used the Recursive Least Square algorithm (RLS) in the ANC to eliminate the ECG noise [8]. The main disadvantage of the RLS algorithm is its very high computational complexity, while it provides fast convergence rate. Even though there were number of advanced signal processing techniques are applied to the study of the noisy ECG signals, such as adaptive filter, wavelet transforms, and independent component analysis [7]. Some of the artifact problems and low signal to noise ratio problems are arise during the filtering of ECG signals may be reduced with the simple, frequency selective filtering techniques. Still it is very important and interesting approach to study about the noisy ECG filtering characteristics.

III. KALMAN FILTER DERIVATION

The Kalman filter is a recursive predictive filter that is based on the use of the recursive algorithms and the state space model techniques. The Kalman filter is developed with a set of mathematical equations that implements a predictor-corrector type estimator. It is an optimal data processing algorithm in the sense that it minimizes the estimated error covariance when some presumed conditions are met [9].

3.1 The Process to Be Estimated:

The Kalman filter is used to solve the problem of estimating the state 'x' of a controlled process that is regulated with the linear stochastic difference equation,

$$x_k = Ax_{k-1} + Bu_k + w_{k-1} \quad (3.1)$$

And with a measurement 'y_k', it is

$$y_k = Hx_k + v_k \quad (3.2)$$

The random variables in above equations w_k and v_k represents the process and measurement noise respectively. These noises are assumed to be white process with normal probability distributions and independent of each other [10],

$$\begin{aligned} p(w) &\sim N(0, Q) \quad \text{and} \\ p(v) &\sim N(0, R) \end{aligned} \quad (3.3)$$

The measurement noise covariance R_k and process noise covariance Q_k matrices may be change with each time step, however here we assume that they are constant.

3.2 The Computational Origins of the Kalman Filter:

We define \hat{x}_k^- as our a priori state estimation at the step k given the information of the process prior to step k, and assume \hat{x}_k^+ our a posteriori state estimate at the step k with given measurement y_k. Then we can define a priori and a posteriori estimate errors as

$$\begin{aligned} e_k &\equiv x_k - \hat{x}_k^- \\ e_k^- &\equiv x_k - \hat{x}_k^- \end{aligned} \quad (3.4)$$

a priori estimate error covariance is given by

$$P_k^- = E[e_k^- e_k^{-T}] \quad (3.5)$$

and a posteriori estimate error covariance is given by

$$P_k = E[e_k e_k^T] \quad (3.6)$$

A posteriori state estimate is given by

$$\hat{x}_k^+ = \hat{x}_k^- + K(y_k - H\hat{x}_k^-) \quad (3.7)$$

The difference in above equation is referred as the residual or measurement innovation. The residual reflect the divergence between the actual measurement and the predicted measurement. The nxm matrix K is chosen to be as the

blending factor or gain that reduces the a posteriori error covariance equation [9]. The resulting gain K_k that minimizes equation (3.7) is given

$$K_k = P_k^- H^T (HP_k^- H^T + R)^{-1} \quad (3.8)$$

3.3 Kalman Filter Algorithm:

The Kalman filter is estimate the process state at a specific time and then it obtains feedback in term of measurement. The Kalman filter equations are categorized into two groups: time update equations and measurement update equations. Time update equations are mainly used for projecting forward in time domain of the current state and error covariance estimate to obtain a priori estimate for the next time step.

Measurement update equations are used for the feedback that means for integrating a new measurement into a priori estimate to obtain an improved a posteriori estimate. Table 3.1 and 3.2 shows specific equations for the time update and measurement update equations.

Table 3.1: Kalman filter time updating equations

$$\hat{x}_k^- = A\hat{x}_{k-1} + Bu_{k-1} \quad (3.9)$$

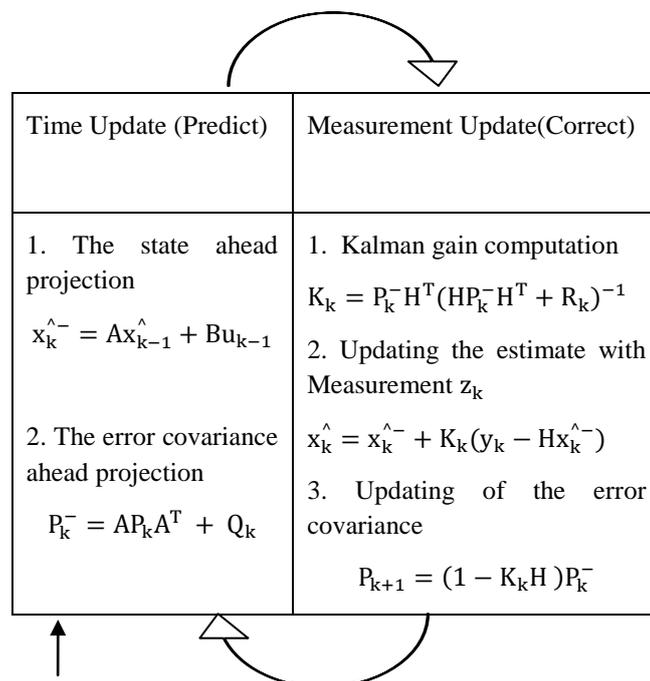
$$P_k^- = AP_k A^T + Q_k \quad (3.10)$$

Table 3.2: Kalman filter time update equations

$$K_k = P_k^- H^T (HP_k^- H^T + R_k)^{-1} \quad (3.11)$$

$$\hat{x}_{k+1} = \hat{x}_k^- + K_k(y_k - H\hat{x}_k^-) \quad (3.12)$$

$$P_{k+1} = (1 - K_k H)P_k^- \quad (3.13)$$



Initial estimation at $k=0$

output values at k will be the inputs for $k+1$

Fig 2: A complete structure of Kalman filters operation.

The first work during the measurement update is to calculate the Kalman gain K_k . Then next step is to actually measuring the process to obtain Z_k , and by integrating the measurement we can generate an a posteriori state estimate. After that the final step is to getting an a posteriori error covariance which is estimating via equation (3.13). After each time and measurement updating pair the process is repeated with the previous a posteriori estimate used for the prediction or projects the new a priori estimate. This algorithmic behavior is one of the very charming features of the Kalman filter that

it makes a practical implementation much more executable than an implementation of a Wiener filter which is used to operate on each estimate for all of the arriving data directly. The Kalman filter uses recursive conditions and the current state estimation on all previous measurements. Figure 4.2 shows a complete representation of the operation of the filter which is combining with the high-level picture of Fig 4.1 with the state equations from table 4.1 and table 4.2.

IV. PRAPOSED ALGORITHM

4.1 Improved Kalman Filter Approach:

The derived Kalman filter implementation is often difficult due to the problem of obtaining a good estimate of the process and measurement noise covariance matrices Q_k and R_k . More research work has been done in this field of getting good estimates of this covariance from data. One of the important and practical approach to get good estimates is the “Auto covariance least squares (ALS)” technique that uses the time lagged auto covariance of routine operating data to estimate the covariance. The error noise covariance noise is calculated by using the ALS is as follows

$$P_{k|k} = cov(x_k - \hat{x}_{k|k}) \quad (3.11)$$

After calculating and collecting the error vectors we get,

$$P_{k|k} = cov((I - K_k H_k)(x_k - \hat{x}_{k|k-1}) - K_k v_k) \quad (3.12)$$

Since the measurement error vector v_k is uncorrelated with the remaining terms, it becomes

$$P_{k|k} = (I - K_k H_k)P_{k|k-1}(I - K_k H_k)^T + K_k R_k K_k^T \quad (3.13)$$

This formula sometimes known as the Joseph form of the covariance update equation and it is valid for any value of K_k . The eq (3.13) is very important if a non-optimal Kalman gain is advisedly used.

$$K_k = P_{k|k} H_k^T (H_k P_{k|k} H_k^T + R_k)^{-1} \quad (3.14)$$

It is straight forward equation to prove that the resultant Kalman gain is increased. Hence, more emphasis is put on newly arriving data. Due to increase in kalman gain the Gaussian noise reduces efficiently and the signal to noise ratio is increases in proposed algorithm compare to the Kalman filter approach.

V. RESULTS

The following figures represent the simulation results for different contaminated noisy ECG signals which are applied to the Kalman filter and Improved Kalman filter.

In Fig.1 ‘clean ECG signal’ shows original ECG signal which is obtained from the MIT-BIH arrhythmia data base. Gaussian white noise is used as the noise source and embedded in the ECG signal. In this study, the Gaussian noise signal is generated by Matlab code awgn.m and the contaminated ECG signal is represented by ‘Noisy ECG signal’ with 18 dB input SNR. The next two signals are output of Kalman filter and IKF approach.

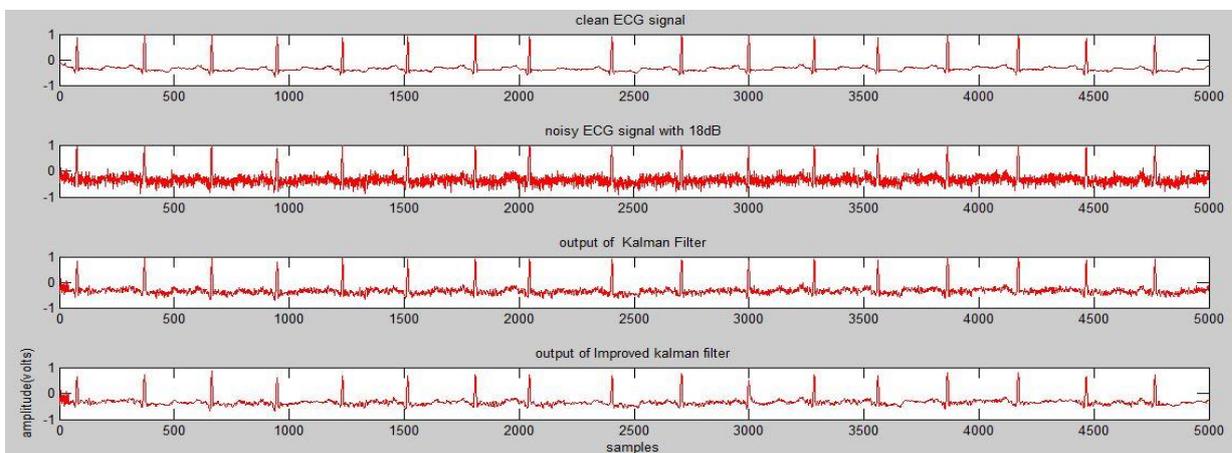


Fig 1: Simulation results of Kalman filter and Improved KF for contaminated noisy ECG signal with input SNR 18dB

In Fig.2 the considered noisy ECG signal is with input SNR is 22dB and corresponding outputs are shown.

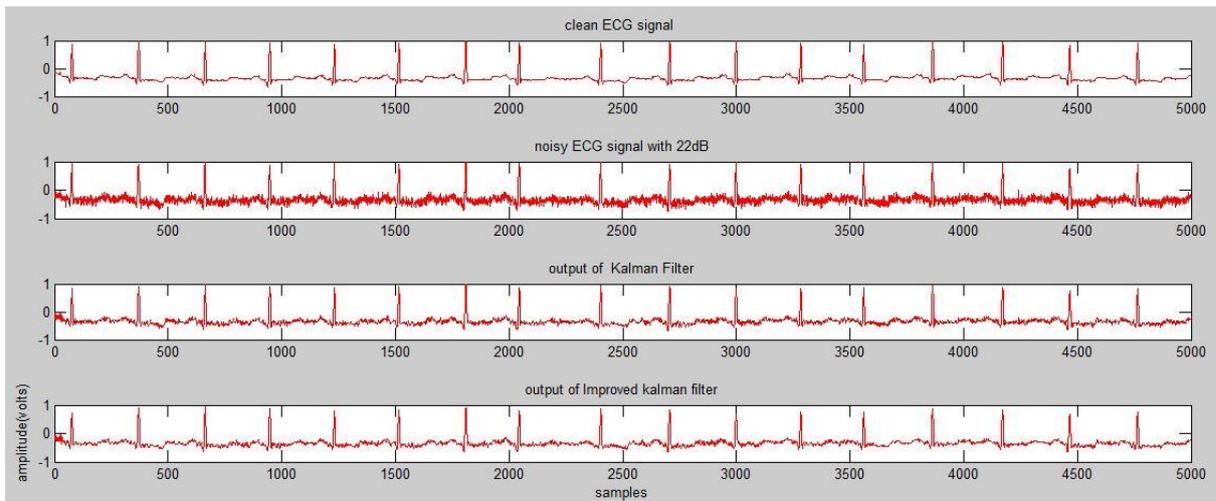


Fig 2: Simulation results of Kalman filter and Improved KF for contaminated noisy ECG signal with input SNR 22dB

In Fig.3 the determined input SNR is 25dB and corresponding outputs for both of the filters are shown.

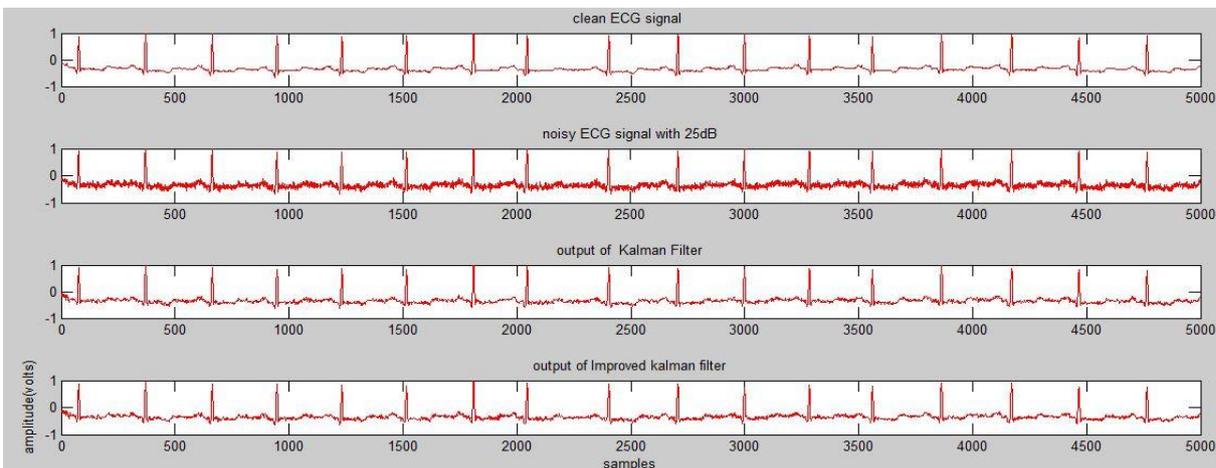


Fig 3: Simulation results of Kalman filter and Improved KF for contaminated noisy ECG signal with input SNR 25dB

In Fig.4 the acquired input signal is the sinus arrest signal. This signal occurs when the SA node stops firing, causes a pause in electrical activity. The seriousness of sinus arrest depends on the length of the pause. The patient will require immediate treatment.

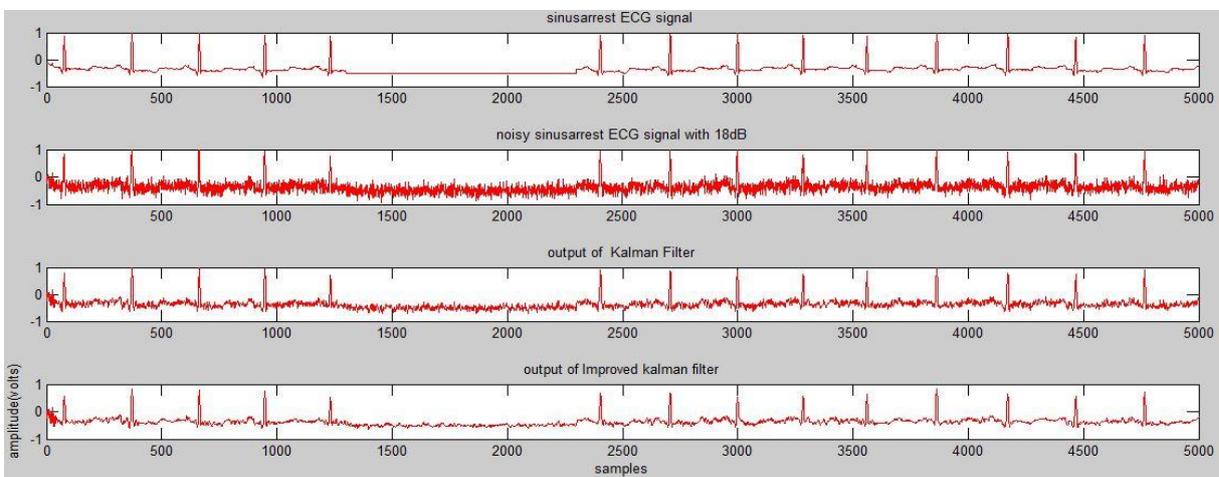


Fig 4: Simulation results of Kalman filter and IKF for noisy sinus arrest ECG signal with input SNR 18dB

In Fig.5 the obtained input signal is the wandering atrial pacemaker (WAP). This signal is a rhythm in which the pacemaker site shifts between the SA node, atria or the AV junction. The P wave configuration changes in appearance during the pacemaker shift. It related to some types of organic heart disease and drug toxicity

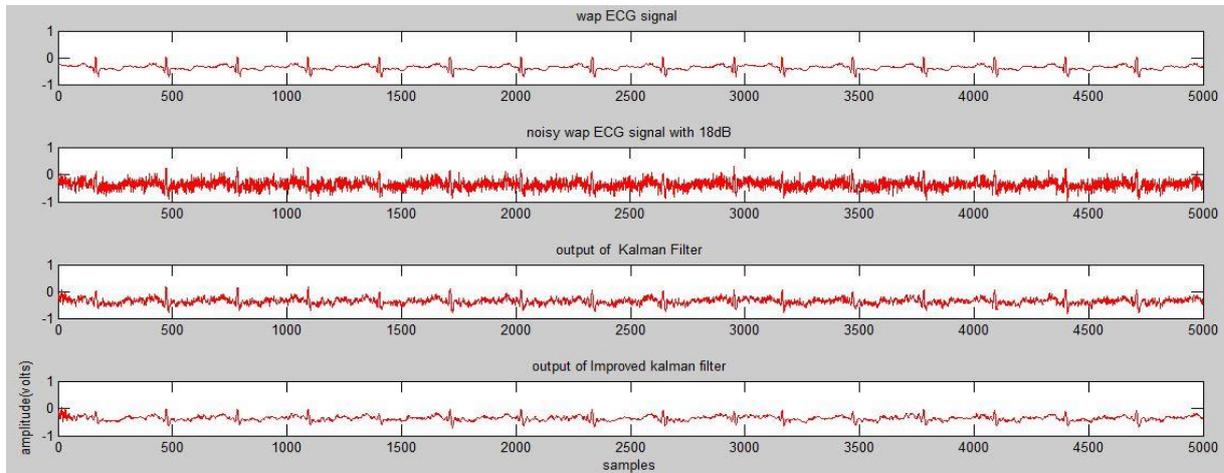


Fig 5: Simulation results of Kalman filter and Improved KF for noisy WAP ECG signal with input SNR 18dB

The summarizing of signal parameters for different contaminated noisy ECG signals for first three figures are shown in table I.

Mean square error (MSE) between filter ECG output and clean ECG was used to measure the filter performance. The lowest MSE value represents better filtering performance. Improved KF algorithm achieves a minimum MSE. The higher SNR values showed less noise part embedded and a cleaner ECG signal.

Table 1: Signal parameters for various contaminated ECG signals with different input SNR

| | 18 db ECG signal | | 22 db ECG signal | | 25 db ECG signal | |
|----------|------------------|-------------|------------------|-------------|------------------|-------------|
| | Kalman Filter | Improved KF | Kalman Filter | Improved KF | Kalman Filter | Improved KF |
| MSE | 0.0046 | 0.0033 | 0.0019 | 0.0018 | 0.0010 | 0.0012 |
| SNR | 23.34 | 29.76 | 29.54 | 34.55 | 33.52 | 42.83 |
| Mean | -0.3343 | -0.33 | -0.3337 | -0.3336 | -0.3334 | -0.3330 |
| Variance | 0.0331 | 0.0285 | 0.0308 | 0.0254 | 0.0298 | 0.0230 |
| STD | 0.1820 | 0.1598 | 0.1754 | 0.1686 | 0.1726 | 0.1717 |

The following table shows the summarizing of signal parameters for abnormal ECG signal such as sinus arrest and wandering atrial pacemaker (WAP).

Table 2: Signal parameters for contaminated ECG signals with 18dB input SNR

| | Noisy ECG signal | | Sinus arrest ECG signal | | WAP ECG signal | |
|----------|------------------|-------------|-------------------------|-------------|----------------|-------------|
| | Kalman Filter | Improved KF | Kalman Filter | Improved KF | Kalman Filter | Improved KF |
| MSE | 0.0046 | 0.0033 | 0.0049 | 0.0032 | 0.0046 | 0.0024 |
| SNR | 23.34 | 29.76 | 24.11 | 29.21 | 21.87 | 28.66 |
| Mean | -0.3343 | -0.33 | -0.3660 | -0.3648 | -0.3620 | -0.3603 |
| Variance | 0.0331 | 0.0285 | 0.0322 | 0.0251 | 0.0135 | 0.0078 |
| STD | 0.1820 | 0.1598 | 0.1794 | 0.1585 | 0.1163 | 0.0884 |

The following graphs show the performance for the both of the kalman filter and improved KF algorithms using different contaminated ECG signals. It shows the better output SNR values. The statistical values are considered from the Table I.

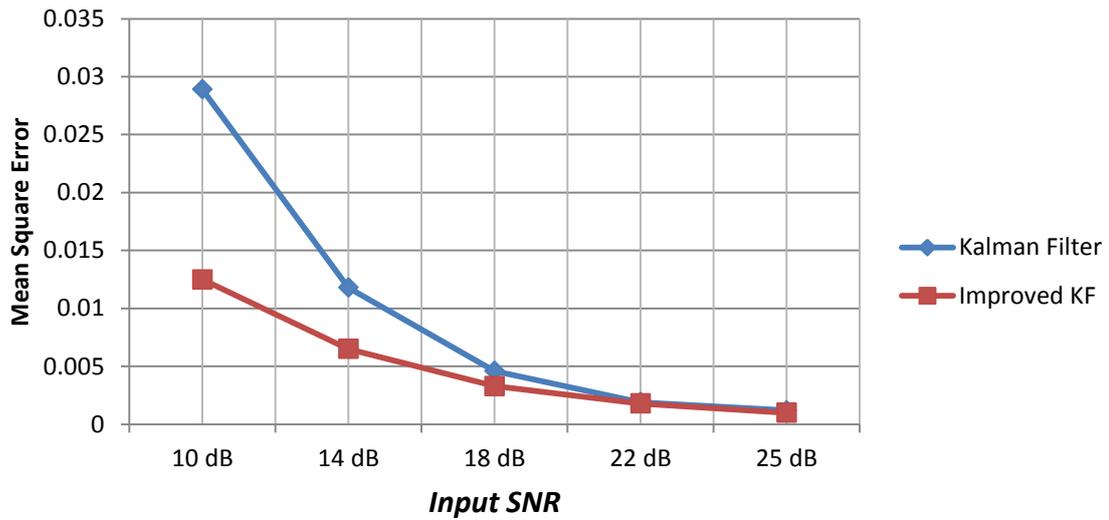


Fig 6: Mean square error values for different contaminated ECG signals

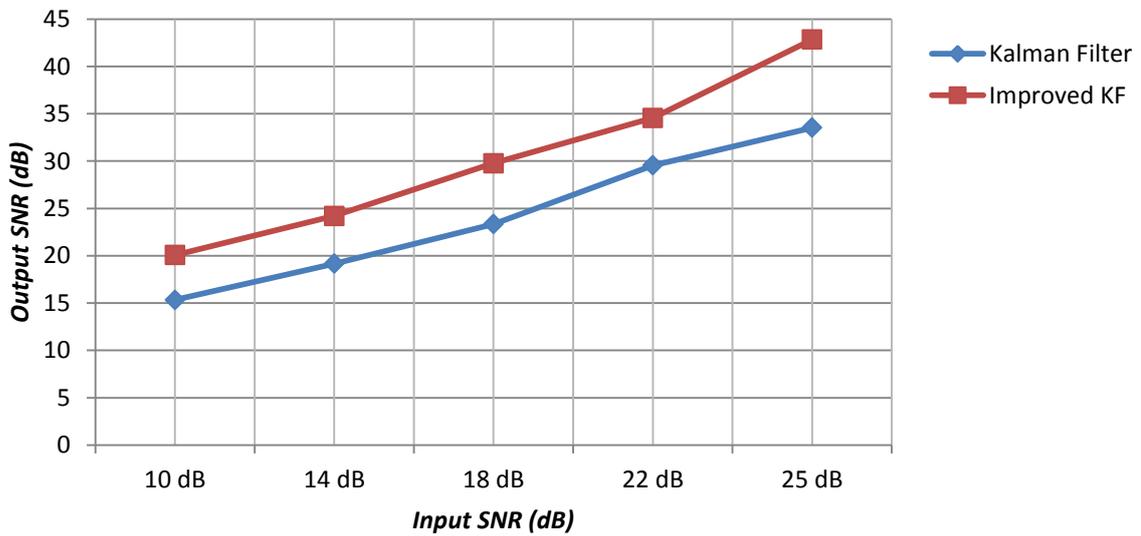


Fig 7: SNR values for different contaminated ECG signals

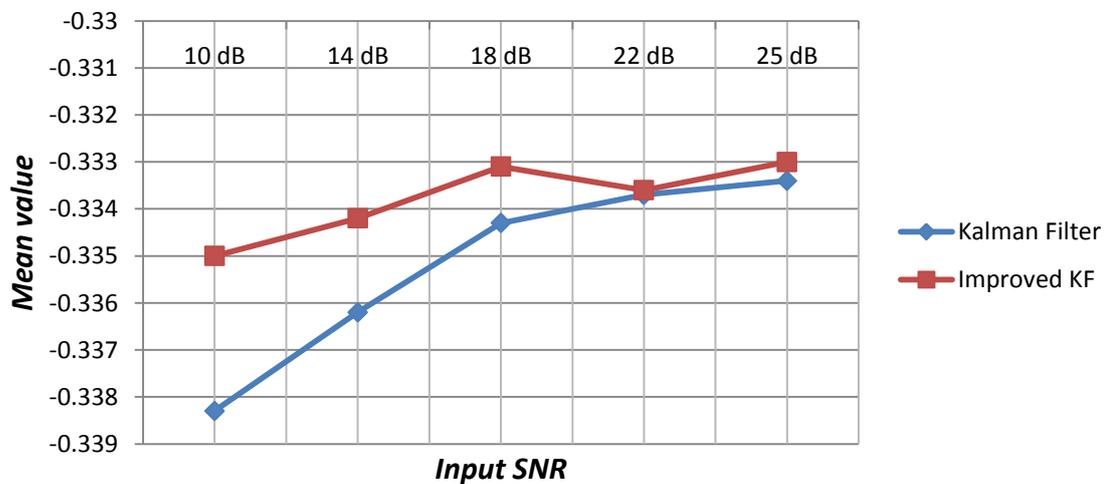


Fig 8: Mean values for different contaminated ECG signals

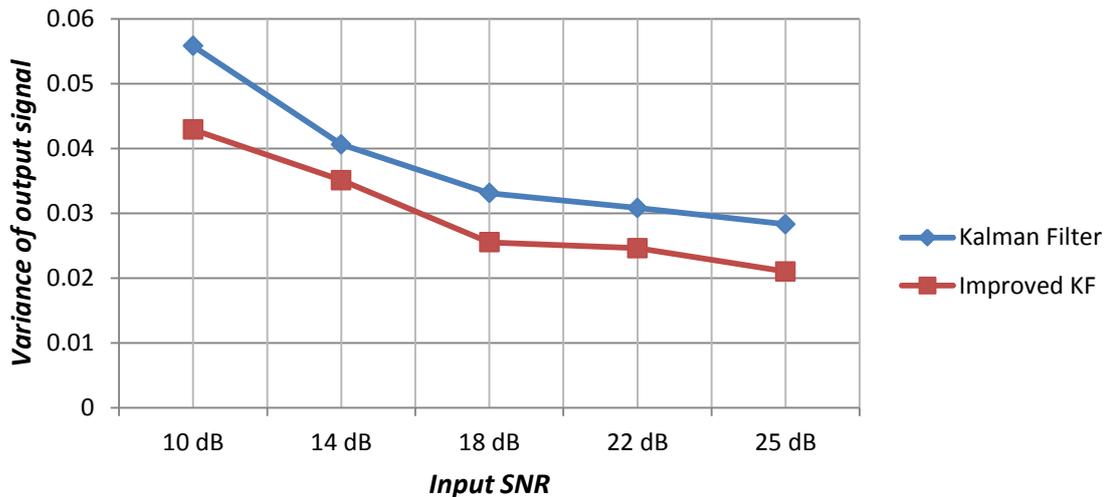


Fig 9: Variance values of the output signal for different contaminated ECG signals

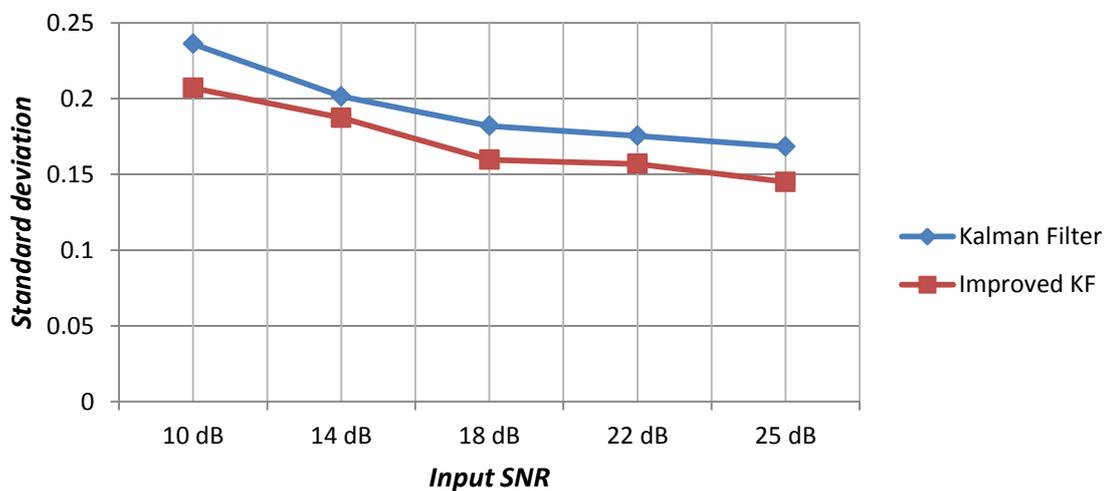


Fig 10: Standard deviation values for different contaminated ECG signals

VI. CONCLUSION

In this theory, the improved Kalman filter has been developed and simulated with the estimation of adaptive noise covariance on different contaminated ECG signals. Also evaluated to assess whether the IK filter has ability to enhancing the SNR value of the signals. At the same time this filter preserves the morphological variations occurred during the recording of the ECG signal. This filter operates with the estimation of the process and measurement noise covariance using ALS technique. This filter has ability to adapt its estimated noise covariance quickly to correspond the output of the filter to the next input. The performance evaluation of this filter is better than a similar derived Kalman filter with the fixed values of process noise covariance.

REFERENCES

- [1] Prakruti J.joshi, Vivek P.Patkar, "ECG denoising using MATLAB" Int. Journal of Scientific & Engineering Research, May-2013
- [2] Manpreet kaur,Birmohan singh, Seema, "Comparison of different approaches for removal of baseline wander from ECG signal", -2011.
- [3] Mbachu C.B. , Offor K.J, "Reduction of power line noise in ECG signal using FIR digital filter implemented with hamming window", Int. Journal of Science, Environment and Technology, 2013.

- [4] Arshdeep Singh, Rajesh Mehra, "Adaptive Filter for ECG Noise Reduction Using RLS Algorithm" Int. Journal of Engineering Research and Applications, Nov-2013.
- [5] R. Sameni, M. Shamsollahi, C. Jutten, and G. Clifford, "A nonlinear bayesian filtering framework for ecg denoising," IEEE Trans. Biomed. Eng., vol. 54, no. 12, pp. 2172–2185, Dec. 2007.
- [6] Bhumika Chandrakar, O.P.Yadav and V.K.Chandra, "A survey of noise removal techniques for ECG signal", Int. Journal of Advanced Research in Computer and Communication Engineerin, March 2013.
- [7] Mostafa Guda, Safa Gasser, "MATLAB Simulation Comparison for Different Adaptive Noise Cancellation Algorithms", the SDIWC in 2014.
- [8] Greg Welch, Gary Bishop, "An Introduction to the Kalman Filter",-2001.
- [9] Paulo A. C. Lopes and Jos'e B. Gerald IST and INESC-ID, "New Normalized LMS Algorithms Based on the Kalman Filter", POSC/EEA-CPS/59401/2004.
- [10] De Freitas, M. Niranjana, and A. Gee, "Hierarchical Bayesian-Kalman models for regularisation and ARD in sequential learning," Dept. Eng., Cambridge Univ., Cambridge, U.K., Tech. Rep., 1998.
- [11] W.Du, H.Cui, K.Tang and Y.Gu , "Modifier formula on mean square convergence of LMS algorithm", Electronics Letters, vol.38, no.19, September 2002.
- [12] A.Jazwinski, "Adaptive filtering", Automatica, - 1969
- [13] S. Martens, R. Sluijter, S.Oei, and J.Bergmans, "Improving QRS detection in multi-channel electrocardiography by principal component analysis," Int. Federation for Medical and Biological Engineering, Prague, Czech Republic, Nov. 2005.

Authors Profile:

D. Venkata Rami Reddy received B.Tech Degree in Electronics & Communication Engineering from JNT University, Ananthapuramu in 2012. He is currently working towards M.Tech Degree in Digital Electronics Communication Systems at Annamacharya Institute of Technology & Sciences, Rajampet, A.P. His research interests include Signal Processing and Communication Systems.

B. Abdul Rahim received B.E Degree in Electronics & Communication Engineering from Gulbarga University in 1990. He received M.Tech (Digital Systems & Computer Electronics) Degree from JNT University, Hyderabad in 2004. He is currently working towards Ph.D. degree from JNT University, Anantapur. At present he is heading the Dept. Of ECE at Annamacharya Institute of technology & sciences, Rajampet, A.P. He has published papers in international journals and conferences. He is a member of professional bodies like IEEE, EIE, ISTE, IACSIT, IAENG etc. His research interests include Fault Tolerant Systems, Embedded Systems and parallel processing. He achieved "Best Teacher Award" for his services by Lions Club, Rajampet India.

Fahimuddin.Shaik received B.Tech Degree in Electronics & Communication Engineering and M.Tech (DECS) from JNT University, Hyderabad, India. He is currently working towards a Ph.D. in biomedical image processing at Rayalaseema University, Kurnool, and India. At present he is an assistant professor in the Department of ECE at the Annamacharya Institute of Technology & Sciences, Rajampet, A.P. His research interests include signal processing, time series analysis, and biomedical image processing. He has presented many research papers at national and international conferences. He has authored a book "MEDICAL IMAGING IN DIABETES, VOL 1- A Technical Approach", Cinnamontal Publishing, December 2011. He is a member in no. of professional bodies like, ISTE, IEI, BMI, IACSIT etc.